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On crystal structure of Cd-Zr intermetallic compounds. By Arunsingh* and B. Dayal, Department of Physics, B.H.U., Varanasi-5, India
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Three compounds of the $\mathrm{Cd}-\mathrm{Zr}$ system were prepared and their crystal structures are reported. A possible reason for the tetragonal to cubic transformation of one of the phases is also given.

The present alloys from metals of widely differing melting points were prepared by compacting, in a narrow capillary tube, appropriate weights of powdered Cd and Zr metals of $99.9 \%$ purity and a 10 amp current at 2 volts was passed through the mixture for about 2 hr . It resulted in the formation of the alloy as a very fine powder.

In all, three intermetallic compounds, viz. $\mathrm{Cd}_{3} \mathrm{Zr}, \mathrm{Cd}_{2} \mathrm{Zr}$ and $\mathrm{Cd}_{2} \mathrm{Zr}_{3}$, were detected and they were studied by the standard powder technique with filtered $\mathrm{Cu} K \alpha$ radiation. The powder photographs were interpreted by the normal procedure and intensity calculations were made. The lattice parameter, density and number of molecules per unit cell are summarized in Table 1.
(i) $\mathrm{Cd}_{3} \mathrm{Zr}$

Out of various possibilities for the Zr and Cd atomic positions for this phase, the one for which the intensities would agree well with the observed intensities is the arrangement in which Zr atoms occupy the corners and Cd atoms are located at the faces. Based on this arrangement we have calculated the intensities which are given in Table 2. The agreement is reasonably good.

The above compound is isostructural with $\mathrm{CuTi}_{3}$ and since the special condition $h+k=2 n$ is satisfied, it is proposed to assign space group $P 4 / \mathrm{mmm}$ to this phase.
(ii) $\mathrm{Cd}_{2} \mathrm{Zr}$

In this case also, various possibilities for atomic positions were tried. Table 3 compares the calculated and observed intensities for this structure. As is evident, the agreement is good. In the proposed structure Zr atoms occupy the cube corners and Cd atoms are at four of the faces, i.e. $\frac{1}{2} 0 \frac{1}{2}$ and $0 \frac{1}{2} \frac{1}{2}$ or equivalent positions.
The probable space groups are $P a_{3}$ or $P n_{3}$ as they satisfy the special condition $h+k, k+l, l+h=2 n$.
(iii) $\mathrm{Cd}_{2} \mathrm{Zr}_{3}$

Many structures were tried for this intermetallic compound, but only the following arrangement of atoms gave consistent results. Here it is presumed that Zr atoms

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Table 2. Observed and calculated ' $d$ ' spacings and intensities for $\mathrm{Cd}_{3} \mathrm{Zr}$

| Line <br> number | Observed <br> ${ }^{e} d$ | Calculated <br> $'^{\prime} d^{\prime}$ | $h k l$ | $I_{\text {calc }}$ <br> $\left(\times 10^{5}\right)$ | $I_{\text {obs }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2.491 | 2.527 | 111 | 30.0 | $V S$ |
| 2 | 2.191 | 2.208 | 200 | 10.3 | $S$ |
| 3 | 2.139 | 2.154 | 002 | 4.8 | $m$ |
| 4 | 1.555 | 1.561 | 220 | 3.37 | $m$ |
| 5 | 1.534 | 1.552 | 202 | 6.4 | $S$ |
| 6 | 1.322 | 1.328 | 131 | 7.5 | $V S$ |
| 7 | 1.299 | 1.304 | 113 | 3.5 | $S$ |
| 8 | 1.258 | 1.264 | 222 | 3.01 | $S$ |
| 9 | 1.101 | 1.104 | 400 | 1.1 | $W$ |
| 10 | 1.074 | 1.076 | 004 | 0.52 | $W$ |
| 11 | 1.010 | 1.012 | 331 | 1.89 | $m$ |
| 12 | 0.9982 | 1.001 | 313 | 3.75 | $S$ |
| 13 | 0.9868 | 0.9875 | 420 | 1.87 | $m$ |
| 14 | 0.9795 | 0.9822 | 402 | 1.87 | $m$ |
| 15 | 0.9692 | 0.9679 | 204 | 1.87 | $m$ |
| 16 | 0.8978 | 0.8974 | 422 | 3.96 | $S$ |
| 17 | 0.8878 | 0.8763 | 224 | 2.0 | $m$ |
| 18 | 0.8484 | 0.8492 | 151 | 4.62 | $S$ |
| 19 | 0.8421 | 0.8426 | 333 | 2.4 | $m$ |
| 20 | 0.8285 | 0.8305 | 115 | 2.19 | $m$ |
| 21 | 0.7810 | 0.7805 | 440 | 4.96 | $S$ |

Table 3. Observed and calculated ' $d$ ' spacings and intensities for $\mathrm{Cd}_{2} \mathrm{Zr}$

| Line <br> number | $d_{\text {obs }}$ | $d_{\text {calc }}$ | $h k l$ | $I_{\text {calc }}$ <br> $\left(\times 10^{5}\right)$ | $I_{\text {obs }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2.566 | 2.572 | 111 | 17 | $V S$ |
| 2 | 2.178 | 2.189 | 200 | 8.3 | $S$ |
| 3 | 1.546 | 1.547 | 220 | 5.4 | $S$ |
| 4 | 1.318 | 1.319 | 113 | 10.3 | $V S$ |
| 5 | 1.265 | 1.264 | 222 | 1.74 | $W$ |
| 6 | 1.094 | 1.094 | 400 | 0.88 | $V W$ |
| 7 | 1.007 | 1.004 | 331 | 3.07 | $S$ |
| 8 | 0.9802 | 0.9787 | 420 | 3.06 | $S$ |
| 9 | 0.8937 | 0.8935 | 422 | 3.25 | $V S$ |
| 10 | 0.8418 | 0.8424 | 333 | 3.93 | $V S$ |
|  |  |  | 115 |  |  |

occupy cube corners and are also situated halfway along the $a$ and $c$ axes. The Cd atoms are located at the centre of the ' $a c$ ' face and at the body centre. The atomic coor-

Table 1. Crystal data

| Compound | Lattice type | $a$ | $b$ | $c$ | Density | Number of mols. <br> per unit cell |
| :---: | :--- | :--- | :---: | :---: | :---: | :---: |
| $\mathrm{Cd}_{3} \mathrm{Zr}$ | Tetragonal | 4.4151 | - | 4.307 | 6.85 | 0.80 |
| $\mathrm{Cd}_{2} \mathrm{Zr}^{2}$ | Cubic | 4.3768 | - | 6.55. | 1.03 |  |
| $\mathrm{Cd}_{2} \mathrm{Zr}_{3}$ | Orthorhombic | 7.86 | 6.52 | 5.30 | 3.69 | 1.2 |

Table 4. Observed and calculated ' $d$ ' spacings and intensities for $\mathrm{Cd}_{2} \mathrm{Zr}_{3}$

| Line number | $d_{\text {obs }}$ | $d_{\text {calc }}$ | hkl | $\begin{gathered} I_{\text {cale }} \\ \left(\times 10^{5}\right) \end{gathered}$ | $I_{\text {obs }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 2.784 | 2.777 | 021 | 2.06 | W |
| 2 | 2.548 | 2.509 | 220 | 24.7 | VS |
| 3 | 2.447 | 2.455 | 012 | $5 \cdot 8$ | $m S$ |
|  |  |  | 310 | ---* |  |
| 4 | 2.337 | 2.375 | 301 | $0 \cdot 12$ | W |
| 5 | 2.214 | $2 \cdot 197$ | 202 | 14.5 | $S$ |
| 6 | 2.162 | $2 \cdot 174$ | 030 | $2 \cdot 0$ | $a$ |
| 7 | 1.888 | 1.902 | 410 | $2 \cdot 6$ | $m S$ |
|  |  | 1.902 | 230 | $2 \cdot 6$ |  |
| 8 | 1.615 | $1 \cdot 617$ | 322 | 0.75 | $m$ |
|  |  | 1.617 | 421 | 0.75 |  |
|  |  | 1.614 | 203 | 0.37 |  |
| 9 | 1.572 | 1.571 | 500 | $0 \cdot 17$ | $m$ |
|  |  | 1.578 | 402 | 4.7 |  |
| 10 | $1 \cdot 549$ | 1.553 | 023 | $0 \cdot 32$ | $m$ |
|  |  | 1.545 | 232 | $2 \cdot 6$ |  |
| 11 | 1.462 | 1.449 | 241 | $0 \cdot 52$ | $m$ |
|  |  | 1.457 | 430 | $1 \cdot 1$ |  |
|  |  | 1.464 | 303 | $0 \cdot 26$ |  |
| 12 | $1 \cdot 366$ | $1 \cdot 368$ | 521 | $0 \cdot 42$ | W |
|  |  | $1 \cdot 371$ | 033 | ---* |  |
| 13 | $1 \cdot 341$ | 1.336 | 323 | 0.38 (?) | $S$ |
|  |  | 1.339 | 341 | 0.38 |  |
| 14 | $1 \cdot 320$ | $1 \cdot 313$ | 403 | $0 \cdot 15$ | $m$ |
|  |  | $1 \cdot 313$ | 004 | 1.24 |  |
| 15 | 1-284 | 1.280 | 610 | 0.68 | W |
|  |  | 1.287 | 413 | $0 \cdot 16$ |  |
| 16 | 1.041 | 1.037 | 115 | 0.09 | W |
|  |  | 1.041 | 424 | $2 \cdot 6$ (?) |  |
|  |  | 1.041 | 153 | 0.09 |  |
|  |  | 1.040 | 334 | 0.09 |  |
|  |  | 1.039 | 721 | $0 \cdot 20$ |  |
|  |  | 1.041 | 542 | $0 \cdot 20$ |  |
| 17 | 1.022 | 1.021 | 712 | ---* | W |
|  |  | 1.023 | 205 | $0 \cdot 10$ |  |
|  |  | 1.023 | 443 | $0 \cdot 20$ |  |
| 18 | 1.010 | 1.014 | 253 | 0.08 | W |
|  |  | 1.010 | 215 | 0.08 |  |
| 19 | 0.9947 | 0.9974 | 730 | $0 \cdot 04$ | W |
|  |  | 0.9950 | 244 | $2 \cdot 5$ (?) |  |
| 20 | 0.9802 | 0.9806 | 731 | 0.08 | VW |
|  |  | 0.9806 | 434 | $0 \cdot 75$ |  |
| 21 | $0 \cdot 9668$ | 0.9658 | 801 | 0.09 | W |
|  |  | 0.9672 | 524 | $0 \cdot 18$ |  |
| 22 | 0.9076 | $0 \cdot 9067$ | 170 | 0.04 | $m$ |
|  |  | 0.9105 | 741 | $0 \cdot 78$ |  |
| 23 | $0 \cdot 8814$ | $0 \cdot 8824$ | 831 | $0 \cdot 09$ | $m$ |
|  |  | 0.8833 | 006 | $0 \cdot 70$ |  |
| 24 | $0 \cdot 8580$ | 0.8584 | 803 | $0 \cdot 11$ | $m$ |
|  |  | 0.8565 | 704 | $0 \cdot 11$ |  |
|  |  | 0.8606 | 544 | $0 \cdot 22$ |  |
|  |  | 0.8553 | 636 | $0 \cdot 86$ |  |

dinates will be as below:

| Zr | 000 | $\frac{1}{2} 00$ | $00 \frac{1}{2}$ |
| :--- | :--- | :--- | :--- |
| Cd | $\frac{1}{2} 0 \frac{1}{2}$ | $\frac{1}{2} \frac{1}{2} \frac{1}{2}$ |  |

In Table 4 are listed the calculated intensities and observed intensities. The agreement between these data is good enough to justify the proposed structure. Other possible arrangements of atoms lead to calculated intensities which are in variance with the observed values and, therefore, the proposed structure seems to represent the correct arrangement of atoms.

Very sharp lines were obtained in the cases of $\mathrm{Cd}_{3} \mathrm{Zr}$ and $\mathrm{Cd}_{2} \mathrm{Zr}$ but the pattern from $\mathrm{Cd}_{2} \mathrm{Zr}_{3}$ was comparatively diffuse.

## Discussion

The structures clearly suggest that it is the Cd atom which diffuses in the Zr matrix because in all three structures we find Zr atoms occupying the corners. As a result of the interdiffusion of Cd atoms the shape and size of the matrix have changed in accordance with the local changes in the energy of the lattice.

We have seen for the tetragonal phase that $c / a=0.97$, which almost corresponds to a strained cube. From density measurements the number of atoms per unit cell is found to be $\sim 0.80$. This suggests that the structures contain voids and that the presence of relatively heavy Cd atoms on the ' $a b$ ' face strains the cube; hence the $c$ axis is compressed and the $a$ axis elongated. We find confirmation of this model in the cubic phase (which is obtained by reducing the Cd content) where removal of the Cd atom from the $a b$ face causes the tetragonal phase to revert to the cubic phase.

It was observed that on holding the tetragonal phase at a higher temperature ( $>250^{\circ} \mathrm{C}$ ) the Cd atom is released by this phase which then transforms itself into the cubic phase (Pietrokowsky, 1954). This further confirms the above contention.

We may mention here that $\mathrm{Cd}_{2} \mathrm{Zr}$ is a valency compound and hence the more stable.

Lastly, $\mathrm{Cd}_{2} \mathrm{Zr}_{3}$ seems to possess a defect structure; hence we may suggest that a few Cd or Zr atoms may be randomly distributed in some cells to give approximately 1.2 atoms per unit cell.

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## Reference

Pietrokowasky, P. (1954). Trans. A.I.M.E. 200, 219.

